PART - A (MATHEMATICS)

SECTION - A

(One Options Correct Type)

This section contains **20 multiple choice questions**. Each question has **four choices** (1), (2), (3) and (4), out of which **ONLY ONE** option is correct.

*1. Let e_1 be the eccentricity of the hyperbola $\frac{x^2}{16} - \frac{y^2}{9} = 1$ and e_2 be the eccentricity of the ellipse $\frac{x^2}{a^2} + \frac{y^2}{b^2} = 1$, a > b, which passes through the foci of the hyperbola. If $e_1e_2 = 1$, then the length of the cord of the ellipse parallel to the x-axis and passes through (0, 2) is:

(1) $\frac{8\sqrt{5}}{3}$

(2) $4\sqrt{5}$

(3) $3\sqrt{5}$

(4) $\frac{10\sqrt{5}}{3}$

Ans. (4)

Sol.
$$e_1 = \sqrt{1 + \frac{9}{16}} = \frac{5}{4} \implies e_2 = 4/5 \implies 1 - \frac{b^2}{a^2} \implies \frac{b}{a} = \frac{3}{5}$$

$$\Rightarrow$$
 Ae₁ = a \Rightarrow 4 $\times \frac{5}{4}$ = a \Rightarrow a = 5

Solving $\frac{x^2}{25} + \frac{y^2}{9} = 1$ with the line y = 2

$$\Rightarrow \frac{x^2}{25} = 1 - \frac{4}{9} \Rightarrow x = \pm \frac{5\sqrt{5}}{3}$$

 \Rightarrow length of chord $|x_2 - x_1| = \frac{10\sqrt{5}}{3}$.

*2. If α , β are the roots of the equation, $x^2 - x - 1$ and $S_n = 2023 \alpha^n + 2024 \beta^n$, then :

(1) $S_{12} = S_{11} + S_{10}$

(2) $2S_{11} = S_{12} + S_{10}$

(3) $2S_{12} = S_{11} + S_{10}$

(4) $S_{11} = S_{10} + S_{12}$

Ans. (1)

Sol.
$$S_n = 2023\alpha^n + 2024\beta^n$$

$$S_{n-1} = 2023\alpha^{n-1} + 2024\beta^{n-1}$$

$$S_{n-2} = 2023\alpha^{n-2} + 2024\beta^{n-2}$$

$$\boldsymbol{S}_n = \boldsymbol{S}_{n-1} + \boldsymbol{S}_{n-2}$$

$$S_{12} = S_{11} + S_{10} \; .$$

Let R be the interior region between the lines 3x - y + 1 = 0 and x + 2y - 5 = 0 containing the origin. The set of all values of a, for which the points $(a^2, a + 1)$ lie in R, is: *3.

$$(1) \quad (-3,-1) \cup \left(-\frac{1}{3},1\right)$$

(2)
$$(-3,0) \cup \left(\frac{1}{3},1\right)$$

(3)
$$(-3,0) \cup \left(\frac{2}{3},1\right)$$

(4)
$$(-3,-1) \cup \left(\frac{1}{3},1\right)$$

Ans.

Sol.
$$3a^2 - (a+1) + 1 > 0$$

$$3a^2 - a > 0 \Rightarrow a(3a - 1) > 0 \Rightarrow (-\infty, 0) \cup \left(0, \frac{1}{3}\right)$$
 ... (i)

$$a^{2} + 3(a + 1) - 5 < 0$$

 $a^{2} + 2a - 3 < 0$
 $a^{2} + 3a - a - 3 < 0$

$$a^2 + 2a - 3 < 0$$

$$a^2 + 3a - a - 3 < 0$$

$$(a + 3)(a - 1) < 0 \Rightarrow a \in (-3, 1)$$

...(ii)

From (i) and (ii)

$$a \in (-3, 0) \cup (1/3, 1)$$

- Let $f: R \left\{-\frac{1}{2}\right\} \to R$ and $g: R \left\{\frac{-5}{2}\right\} \to R$ be defined as 4.
 - $f(x) = \frac{2x+3}{2x+1}$ and $g(x) = \frac{|x|+1}{2x+5}$. Then. The domain of the function fog is:

(1)
$$R - \left\{-\frac{7}{4}\right\}$$

(2)
$$R - \left\{-\frac{5}{2}\right\}$$

(3)
$$R - \left\{-\frac{5}{2}, -\frac{7}{4}\right\}$$

Ans. **(2)**

Sol.
$$f(g(x)) = \frac{2 \cdot (g(x)) + 3}{2(g(x)) + 1} = \frac{2 \cdot (\frac{|x| + 1}{2x + 5}) + 3}{2(\frac{|x| + 1}{2x + 5}) + 1}$$

$$=\frac{2\big(\big|x\big|+1\big)+3\big(2x+5\big)}{2\big(\big|x\big|+1\big)+2x+5}=\frac{2\big|x\big|+2+6x+15}{2\big|x\big|+2+2x+5}$$

$$=\frac{2|x|+6x+17}{2|x|+2x+7}$$

$$\frac{8x+17}{4x+7}\,, \text{ if } x \geq 0,\\$$

$$\frac{4x+17}{7}$$
, if $x < 0$.

5. The values of
$$\alpha$$
, for which
$$\begin{vmatrix} 1 & \frac{3}{2} & \alpha + \frac{3}{2} \\ 1 & \frac{1}{3} & \alpha + \frac{1}{3} \\ 2\alpha + 3 & 3\alpha + 1 & 0 \end{vmatrix} = 0$$
, lie in the interval

$$(1) \quad \left(-\frac{3}{2},\frac{3}{2}\right)$$

$$(4)$$
 $(-2, 1)$

Ans. (2)

Sol.

$$C_{3} \to C_{3} - (\alpha C_{1} + C_{2})$$

$$\begin{vmatrix}
1 & \frac{3}{2} & 0 \\
1 & \frac{1}{3} & 0 \\
2\alpha + 3 & 3\alpha + 1 & -(2\alpha^{2} + 6\alpha + 1)
\end{vmatrix} = 0$$

$$\Rightarrow \quad \frac{7}{6} \Big(2\alpha^2 + 6\alpha + 1 \Big) = 0 \quad \alpha = \frac{-3 + \sqrt{7}}{2}, \, \frac{-3 - \sqrt{7}}{2} \, .$$

6. If
$$\lim_{x\to 0} \frac{3+\alpha \sin x + \beta \cos x + \log_e \left(1-x\right)}{3 \tan^2 x} = \frac{1}{3}$$
, then $2\alpha - \beta$ is equal to : (2) 1

Ans.

Sol.
$$\lim_{x \to 0} \frac{3 + \alpha \sin x + \beta \cos x + \log_{e} (1 - x)}{3 \tan^{2} x} = \frac{1}{3}$$

$$\frac{3 + \alpha \left(x - \frac{x^{3}}{3}\right) + \beta \left(1 - \frac{x^{2}}{2}\right) + \left(-x + \frac{x^{2}}{2}\right)}{3x^{2}} = \frac{1}{3}.$$

$$3 + \beta = 0$$

$$\beta = -3$$

$$2\alpha - \beta = 5.$$

$$\alpha - 1 = 0$$

$$\alpha = + 1$$

- 7. Let $g(x) = 3f(\frac{x}{3}) + f(3-x)$ and f''(x) > 0 for all $x \in (0, 3)$. If g is decreasing in $(0, \alpha)$ and increasing in $(\alpha, 3)$, then 8α is:
 - (1) 24

(2) 18

(3) 0

(4) 20

Ans. (2)

Sol.
$$g(x) = 3f\left(\frac{x}{3}\right) + f(3-x)$$
$$g'(x) = 3f'\left(\frac{x}{3}\right) \cdot \frac{1}{3} - f'(3-x)$$
$$= f'\left(\frac{x}{3}\right) - f'(3-x)$$

$$g'(x) < 0, f'\left(\frac{x}{3}\right) - f'(3-x) < 0$$
$$f'\left(\frac{x}{3}\right) < f'(3-x)$$

$$\frac{x}{3} > 3 - x$$

$$\frac{x}{3} + x > 3 \Rightarrow \frac{4x}{3} > 3, x > \frac{9}{4}$$

$$\alpha = \frac{9}{4} = 18.$$

8. If y = y(x) is the solution curve of the differential equation $(x^2 - 4)dy - (y^2 - 3y)dx = 0$, x > 2, $y(4) = \frac{3}{2}$ and the slope of the curve is never zero, then the value of y(10) equals:

(1)
$$\frac{3}{1+2\sqrt{2}}$$

(2)
$$\frac{3}{1+(8)^{1/4}}$$

(3)
$$\frac{3}{1-(8)^{1/4}}$$

(4)
$$\frac{3}{1-2\sqrt{2}}$$

Ans. (2)

Sol.
$$(x^2 - 4)dy - (y^2 - 3y)dx = 0, x > 2, y(4) = \frac{3}{2}$$

$$\int \frac{dy}{y^2 - 3y} = \int \frac{dx}{x^2 - y}$$

$$\frac{1}{3} \int \frac{y - (y - 3)}{y (y - 3)} dy = \int \frac{dx}{x^2 - 2^2}$$

$$\frac{1}{3} \left(\ln \left(y - 3 \right) - \ln y \right) = \frac{1}{4} \ln \left| \frac{x - 2}{x + 2} \right| + c$$

$$\frac{1}{3} \ln \left(\left| \frac{y - 3}{y} \right| \right) = \frac{1}{4} \ln \left| \frac{x - 2}{x + 2} \right| + c$$

$$x = 4, y = 3/2$$

$$\frac{1}{3} \ln \left(\left| \frac{3}{2} - 3 \right| \right) = \frac{1}{4} \left(\left| \frac{4 - 2}{4 + 2} \right| \right) + c$$

$$\Rightarrow c = -\frac{1}{4} \ln \frac{1}{3}.$$

$$\frac{1}{3} \ln \left| \left(\frac{y - 3}{y} \right) \right| = \frac{1}{4} \ln \left| \left(\frac{x - 2}{x + 2} \right) \right| - \frac{1}{4} \ln \frac{1}{3}$$

$$x = 10$$

$$\frac{1}{3} \ln \left(\frac{y - 3}{y} \right) = \frac{1}{4} \ln \left(\frac{8}{12} \right) - \frac{1}{4} \ln \frac{1}{3}$$

$$= \frac{1}{4} \left[\ln \frac{2}{3} - \ln \frac{1}{3} \right]$$

$$\frac{1}{3} \ln \left| \frac{y - 3}{y} \right| = \frac{1}{4} [\ln 2]$$

$$\ln \left| \left(\frac{y - 3}{y} \right) \right| = \frac{3}{4} \ln 2 = \ln (2^{3/4}) = \ln (8^{1/4})$$

$$\Rightarrow \frac{-y + 3}{y} = 8^{1/4} \Rightarrow y = \frac{3}{1 + 8^{1/4}}.$$

The 20th term from the end of the progression 20, $19\frac{1}{4}$, $18\frac{1}{2}$, $17, \frac{3}{4}, ..., -129\frac{1}{4}$ is: *9.

$$(2) - 110$$

$$(1) - 118$$
 $(3) - 100$

$$(4) - 115$$

Sol. 20,
$$\frac{77}{4}$$
, $\frac{37}{2}$, $\frac{71}{4}$, ..., $-\frac{129 \times 4 + 1}{4} = -\frac{517}{4}$
Let $a = -\frac{517}{4}$, $d = \frac{3}{4}$
 $t_{20} = -\frac{517}{4} + 19 \times \frac{3}{4} = -\frac{460}{4} = -115$.

For 0 < a < 1, the value of the integral $\int_{0}^{\pi} \frac{dx}{1 - 2a\cos x + a^{2}}$ is: 10.

(1)
$$\frac{\pi^2}{\pi + a^2}$$

(2)
$$\frac{\pi}{1+a^2}$$

(3)
$$\frac{\pi}{1-a^2}$$

(4)
$$\frac{\pi^2}{\pi - a^2}$$

Sol.
$$I = \int_{0}^{\pi} \frac{dx}{1 - 2a\cos x + a^2}$$

$$I = \int_{0}^{\pi} \frac{dx}{1 + a^{2} - 2a \left(\frac{1 - \tan^{2} \frac{x}{2}}{1 + \tan^{2} \frac{x}{2}}\right)} \int_{0}^{\pi} \frac{\sec^{2} \frac{x}{2}}{\left(1 + a^{2} \left(1 + \tan^{2} \frac{x}{2}\right) - 2a \left(1 + \tan^{2} \frac{x}{2}\right)\right)} dx$$

If
$$\tan \frac{x}{2} = t$$
, $\frac{1}{2} \sec^2 \frac{x}{2} dx = dt$

$$2\int\limits_0^\infty \frac{dt}{\left(1+a^2\right)\!\left(1+t^2\right)\!-2a\!\left(1-t^2\right)}$$

$$2\int\limits_{0}^{\infty} \frac{dt}{t^{2}\left(1+a^{2}+2a\right)+\left(1+a^{2}-2a\right)}$$

$$2\int\limits_{0}^{\infty}\frac{dt}{t^{2}\left(a+1\right)^{2}+\left(1-a\right)^{2}}$$

$$\frac{2}{(a+1)^2} \int_{0}^{\infty} \frac{dt}{t^2 + \left(\frac{1-a}{a+1}\right)^2}$$

$$\frac{2}{\left(a+1\right)^{2}} \cdot \frac{1}{\left(\frac{1-a}{a+1}\right)} \cdot \left(tan^{-1} \left(\frac{t}{\left(\frac{1-a}{a+1}\right)}\right)\right)^{\infty}, \quad \frac{2}{\left(a+1\right)\left(1-a\right)} \left(\frac{\pi}{2}-0\right) = \frac{\pi}{1-a^{2}}.$$

11. Consider the function
$$f:(0, 2) \to R$$
 defined by $f(x) = \frac{x}{2} + \frac{2}{x}$ and the function $g(x)$ defined

- (1) g is not continuous for all $x \in (0, 2)$
- (2) g is continuous and differentiable for all $x \in (0, 2)$
- (3) g is continuous but not differentiable at x = 1
- (4) g is neither continuous nor differentiable at x = 1

Ans. (3)

Sol.
$$f(x) = \frac{x}{2} + \frac{2}{x}$$

 $f'(t) = \frac{1}{2} - \frac{2}{t^2} = 0$

$$\begin{split} &\frac{t^2-4}{2t^2}=0 \ \Rightarrow t=\pm\,2,\\ &\frac{\left(t-2\right)\left(t+2\right)}{2t^2} \ \Rightarrow f(t) \text{ is decreasing in } (0,\,2)\\ &g(x) = \begin{cases} \frac{x}{2} + \frac{2}{x}, & 0 < x \leq 1\\ \frac{3}{2} + x, & kx < 2 \end{cases}, \quad g'(x) = \begin{cases} \frac{1}{2} - \frac{2}{x^2}, & 0 < x \leq 1\\ 1 & 1 < x < 0 \end{cases}. \end{split}$$

*12. Let
$$\alpha = \frac{\left(4!\right)!}{\left(4!\right)^{3!}}$$
 and $\beta = \frac{\left(5!\right)!}{\left(5!\right)^{4!}}$. Then :

(1) $\alpha \in \mathbb{N}$ and $\beta \in \mathbb{N}$

(2) $\alpha \notin N$ and $\beta \in N$

(3) $\alpha \in \mathbb{N}$ and $\beta \notin \mathbb{N}$

(4) $\alpha \notin \mathbb{N}$ and $\beta \notin \mathbb{N}$

Ans. (3)

Sol.
$$\alpha = \frac{(4!)!}{(4!)^{3!}}, \beta = \frac{(5!)!}{(5!)^{4!}}$$

$$\alpha = \frac{24!}{(24)^{3!}}, \beta = \frac{120!}{(120)^{4!}} \Rightarrow \alpha \in \mathbb{N}, \beta \in \mathbb{N}.$$

- *13. Let A and B be two finite sets with m and n elements respectively. The total number of subsets of the set A is 56 more than the total number of subsets of B. Then the distance of the point P(m, n) form the point Q(-2, -3) is:
 - (1) 4

(2) 6

(3) 10

(4) 8

Ans. (3)

Sol. Total subset and
$$A = 2^m$$

Total subset and $B = 2^n$
 $2^m - 2^n = 56$
 $M = 6, n = 3$

$$= \sqrt{(6+2)^2 + (3+3)^2} = \sqrt{64+36} = 10$$

- 14. An urn contains 6 white and 9 black balls. Two successive draws of 4 balls are made without replacement. The probability, that the first draw gives all white balls and the second draw gives all black balls, is:
 - (1) $\frac{5}{256}$

(2) $\frac{3}{715}$

(3) $\frac{3}{256}$

(4) $\frac{5}{715}$

Ans. (2)

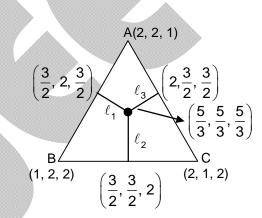
Sol.
$$\frac{{}^{6}C_{4}}{{}^{15}C_{4}} \times \frac{{}^{9}C_{4}}{{}^{11}C_{4}} = \frac{6!}{4! \times 2! \times \frac{15!}{4! \times 11!}} \times \frac{9!}{4! \times 5! \times \frac{11!}{4! \times 7!}}$$
$$= \frac{3}{715}.$$

- Let the position vectors of the vertices A, B and C of a triangle be $2\hat{i} + 2\hat{j} + \hat{k}$, $\hat{i} + 2\hat{j} + 2\hat{k}$ 15. and $2\hat{i} + \hat{j} + 2\hat{k}$ respectively. Let I_1 , I_2 and I_3 be the lengths of perpendiculars drawn from the orthocenter of the triangle on the sides AB, BC and CA respectively, then $l_1^2 + l_2^2 + l_3^2$ equals:
 - (1) 1/3
 - (3) 1/5

(2) 1/2(4) 1/4

Ans.

Sol. $\ell_1 = \sqrt{\left(\frac{5}{3} - \frac{3}{2}\right)^2 + \left(\frac{5}{3} - \frac{3}{2}\right)^2 + \left(\frac{5}{3} - 2\right)^2}$ $=\sqrt{\frac{1}{36}}+\frac{1}{36}+\frac{1}{9}=\frac{1}{\sqrt{6}}$ $\ell_1^2 = \frac{1}{6}$ $\ell_1^2 + \ell_2^2 + \ell_3^2 = 3 \cdot \frac{1}{6} = \frac{1}{2}$



- Let the image of the point (1, 0, 7) in the line $\frac{x}{1} = \frac{y-1}{2} = \frac{z-2}{3}$ be the point (α , β , γ). Then 16. which one of the following points lies on the line passing through $(\alpha,\;\beta,\;\gamma)$ and making angles $\frac{2\pi}{3}$ and $\frac{3\pi}{4}$ with y-axis and z-axis respectively and an acute angle with x-axis?
 - (1) $\left(1, -2, 1+\sqrt{2}\right)$

(2) $(3, 4, 3-2\sqrt{2})$

(3) $(3,-4,3+2\sqrt{2})$

(4) $(1,2,1-\sqrt{2})$

Ans.

- Image is 1, 6, 3 and point satisfying the line $(3, 4, 3 2\sqrt{2})$ Sol.
- The integral $\int \frac{\left(x^8 x^2\right)}{\left(x^{12} + 3x^6 + 1\right) tan^{-1} \left(x^3 + \frac{1}{x^3}\right)} dx$ is equal to: 17.

 - (1) $\log_{e} \left(\left| \tan^{-1} \left(x^{3} + \frac{1}{x^{3}} \right) \right|^{1/2} + C \right)$ (2) $\log_{e} \left(\left| \tan^{-1} \left(x^{3} + \frac{1}{x^{3}} \right) \right|^{1/3} + C \right)$
 - (3) $\log_{e} \left(\left| \tan^{-1} \left(x^{3} + \frac{1}{x^{3}} \right) \right|^{3} + C \right)$ (4) $\log_{e} \left(\left| \tan^{-1} \left(x^{3} + \frac{1}{x^{3}} \right) \right| \right) + C$

Sol.
$$I = \int \frac{\left(x^8 - x^2\right)}{\left(x^{12} + 3x^6 + 1\right) \tan^{-1}\left(x^3 + \frac{1}{x^3}\right)} dx$$

$$I = \int \frac{x^2 - \frac{1}{x^4} dx}{\left(x^6 + 3 + \frac{1}{x^6}\right) \tan^{-1}\left(x^3 + \frac{1}{x^3}\right)}$$

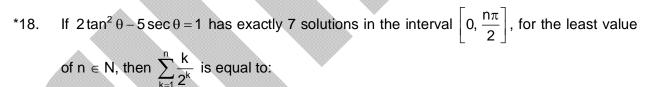
$$I = \int \frac{x^2 - \frac{1}{x^4} dx}{\left(\left(x^3 + \frac{1}{x^3} \right)^2 + 1 \right) tan^{-1} \left(x^3 + \frac{1}{x^3} \right)}$$

$$\tan^{-1}\left(x^3 + \frac{1}{x^3}\right) = t$$

$$\frac{1}{\left(x^{3} + \frac{1}{x^{3}}\right)^{2} + 1} \left(3x^{2} - \frac{3}{x^{4}}\right) dx = dt$$

$$I = \frac{1}{3} \int \frac{dt}{t} = \frac{1}{3} In \left| t \right|$$

$$I = \ln \left| \tan^{-1} \left(x^3 + \frac{1}{x^3} \right) \right|^{1/3} + C$$



(1)
$$1-\frac{15}{2^{13}}$$

(2)
$$\frac{1}{2^{15}} (2^{14} - 14)$$

(3)
$$\frac{1}{2^{13}} (2^{14} - 15)$$

(4)
$$\frac{1}{2^{14}} (2^{15} - 15)$$
.

Ans. (3)

Sol.
$$2 \tan^2 \theta - 5 \sec \theta = 1$$

$$2\sec^2\theta - 2 - 5\sec\theta = 1$$

$$2\sec^2\theta - 5\sec\theta - 3 = 0$$

$$\big(\sec\theta-3\big)\big(2\sec\theta+1\big)=0$$

$$\sec \theta = 3, \frac{-1}{2}$$
 not possible. n = 13

$$S = \frac{1}{2} + \frac{2}{2^2} + \frac{3}{2^3} + \dots \frac{13}{2^{13}}$$

$$\begin{split} &\frac{1}{2}S = \frac{1}{2^2} + \frac{2}{2^3} + \dots \frac{12}{2^{13}} + \frac{13}{2^{14}} \\ &\frac{1}{2}S = \left(\frac{1}{2} + \frac{1}{2^2} + \frac{1}{2^3} + \dots + \frac{1}{2^{13}}\right) - \frac{13}{2^{14}} \\ &\frac{1}{2}S = \frac{1}{2} \left(\frac{1 - \left(\frac{1}{2}\right)^{13}}{1 - \frac{1}{2}}\right) - \frac{13}{2^{14}} \\ &\frac{1}{2}S = 1 - \frac{1}{2^{13}} - \frac{13}{2^{14}} = \frac{2^{14} - 2 - 13}{2^{14}}. \\ &S = \frac{2^{14} - 15}{2^{13}}. \end{split}$$

- 19. The position vectors of the vertices A, B and C of a triangle are $2\hat{i} 3\hat{j} + 3\hat{k}$, $2\hat{i} + 2\hat{j} + 3\hat{k}$ and $-\hat{i} + \hat{j} + 3\hat{k}$ respectively. Let I denotes the length of the angle bisector AD of \angle BAC where D is on the line segment BC, then $2l^2$ equals:
 - (1) 45

(2) 50

(3) 49

(4) 42

Sol.
$$AB = 5$$
, $AC = 5$

D mid point of BC as AB = AC

$$D = \left(\frac{1}{2}, \frac{3}{2}, 3\right)$$

$$\ell = AD = \sqrt{\frac{9}{4} + \frac{81}{4}}$$

$$2\ell^2 = 2 \cdot \frac{90}{4} = 45 \ .$$

- *20. Considering only the principal values of inverse trigonometric functions, the number of positive real values of x satisfying $\tan^{-1}(x) + \tan^{-1}(2x) = \frac{\pi}{4}$ is:
 - (1) 2

(2) more than 2

(3) 0

(4) 1

Ans. (1)

Sol. $\tan^{-1} x + \tan^{-1} 2x = \frac{\pi}{4}$

$$\tan^{-1}\left(\frac{x+2x}{1-2x^2}\right) = \frac{\pi}{4}$$

$$\frac{3x}{1-2x^2} = 1$$

$$3x = 1 - 2x^2$$

$$\begin{aligned} &2x^2 + 3x - 1 = 0 \\ &x = \frac{-3 \pm \sqrt{9 + 8}}{2} = \frac{-3 \pm \sqrt{17}}{2}, \, \frac{-3 + \sqrt{17}}{2}, \frac{-3 - \sqrt{17}}{2} \\ &x = \frac{\sqrt{17} - 3}{2} \end{aligned}$$

SECTION - B

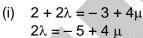
(Numerical Answer Type)

This section contains **10** Numerical based questions. The answer to each question is rounded off to the nearest integer value.

21. The lines $\frac{x-2}{2} = \frac{y}{-2} = \frac{z-7}{16}$ and $\frac{x+3}{4} = \frac{y+2}{3} = \frac{z+2}{1}$ intersect at the point P. If the distance of P from the line $\frac{x+1}{2} = \frac{y-1}{3} = \frac{z-1}{1}$ is I, then $14l^2$ is equal to _____

Ans. 108

Sol.
$$\frac{x-2}{2} = \frac{y}{-2} = \frac{z-7}{16}$$
 any one line $(2+2\lambda, -2\lambda, 7+16\lambda)$ $\frac{x+3}{4} = \frac{y+2}{3} = \frac{z+2}{1}$ any one line $(-3+4\mu, -2+3\mu, -2+\mu)$ Point of intersection



(ii)
$$-2\lambda = -2 + 3\mu$$

 $2\lambda = 2 - 3\mu$

From (i) & (ii)
$$2 - 3\mu = -5 + 4\mu$$

 $\mu = 1$

Point of intersection (1, 1, -1)

$$\mathsf{DR}(\mathsf{PD}) \ = -\ 2 + 2\delta,\ 3\delta,\ 2 + \delta$$

PD perpendicular to line
$$2(-2 + 2\delta) + 3(3\delta) + 2(2 + \delta) = 0$$

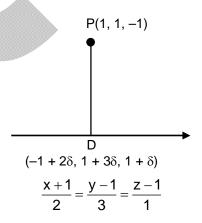
- 4 + 4\delta + 9\delta + 2 + \delta = 0

$$14\delta = 2$$

$$\delta = 1/7$$

PD =
$$\ell = \sqrt{\left(-2 + \frac{2}{7}\right)^2 + \left(\frac{3}{7}\right)^2 + \left(2 + \frac{1}{7}\right)^2}$$

 $\ell^2 = \frac{144}{49} + \frac{9}{49} + \frac{225}{49} = \frac{378}{49} = \frac{54}{7}$
 $14\ell^2 = 108$.



- *22. The mean and standard deviation of 15 observations were found to be 12 and 3 respectively. On rechecking it was found that an observation was read as 10 in place of 12. If μ and σ^2 denote that mean and variance of the correct observations respectively, then $15(\mu + \mu^2 + \sigma^2)$ is equal to _____
- Ans. 2521

Sol.
$$\frac{\sum x_i}{15} = 12 \Rightarrow \sum x_i = 180$$

$$\frac{\sum x_i^2}{15} - (12)^2 = 9 \Rightarrow \sum x_i^2 = 2295$$
Actual:
$$\sum x_i = 182, \sum x_i^2 = 2339$$

$$\sigma^2 = \frac{2339}{15} - \mu^2$$

$$\sigma^2 + \mu^2 = \frac{2339}{15}$$

$$\Rightarrow 15(\mu + \mu^2 + \sigma^2) = 15(\frac{182}{15} + \frac{2339}{15}) = 2521.$$

- *23. The coefficient of x^{2012} in the expansion $(1-x)^{2008} (1+x+x^2)^{2007}$ is equal to _____
- Ans. 0

Sol. Coefficient of
$$x^{2012}$$
 in $(1-x)^{2008}$ $(1+x+x^2)^{2007}$ $(1-x)(1-x^3)^{2007}$
 $\Rightarrow x^{2012}$ in $(1-x^3)^{2007}$ + coefficient of x^{2011} in $(1-x^3)^{2007}$
 $\Rightarrow 0-0=0$.

- 24. If the sum of squares of all real values of α , for which the lines 2x y + 3 = 0, 6x + 3y + 1 = 0 and $\alpha x + 2y 2 = 0$ do not form a triangle is p, then the greatest integer less than or equal to p is _____
- Ans. 32

Sol. Not triangle (i) concurrent

$$\begin{vmatrix} 2 & -1 & 3 \\ 6 & 3 & 1 \\ \alpha & 2 & -2 \end{vmatrix} = 0$$

$$2(-6-2)+1(-12-\alpha)+3(12-3\alpha)=0$$

-16-12-\alpha+36-9\alpha=0

$$10\alpha = 8, \alpha = 4/5.$$

(ii)
$$ax + 2y - 2 = 0$$
 parallel to $2x - y + 3 = 0$

$$-\frac{a}{2} = 2$$
, $a = -4$

(iii)
$$ax + 2y - 2 = 0$$
 parallel to $6x + 3y + 1 = 0$
 $\frac{a}{6} = \frac{2}{3}$, $a = 4$

$$P = \left(\frac{4}{5}\right)^{2} + \left(4\right)^{2} + \left(-4\right)^{2}$$

$$P = 16 + 16 + \frac{16}{25} = 32 + \frac{16}{25}$$

$$[P] = 32.$$

25. Let $f(x) = \int_0^x g(t) \log_e \left(\frac{1-t}{1+t}\right)$ dt, where g is a continuous odd function. If $\int_{-\pi/2}^{\pi/2} \left(f(x) + \frac{x^2 \cos x}{1+e^x}\right) dx = \left(\frac{\pi}{\alpha}\right)^2 - \alpha$, then α is equal to

Ans. 2

Sol.
$$f(x) = \int_{0}^{x} g(t) \log_{e} \left(\frac{1-t}{1+t}\right) dt$$

g(t) . $ln\left(\frac{1-t}{1+t}\right) = odd function \times odd function = even function$

f(x) = Integration of even function = odd function.

$$\int_{-\pi/2}^{\pi/2} \left(f(x) + \frac{x^2 \cos x}{1 + e^x} \right) dx = \int_{-\pi/2}^{\pi/2} f(x) dx + \int_{-\pi/2}^{\pi/2} \frac{x^2 \cos x}{1 + e^x} dx$$

$$I = 0 + \int_{-\pi/2}^{\pi/2} \frac{x^2 \cos x}{1 + e^x} dx$$
 ...(i)

$$I = \int_{-\pi/2}^{\pi/2} \frac{\left(-x\right)^2 \left(\cos\left(-x\right)\right)}{1 + e^{-x}} dx = \int_{-\pi/2}^{\pi/2} \frac{e^x x^2 \cos x}{1 + e^x} dx \dots (ii)$$

Add (i) & (ii)

$$2I = \int_{-\pi/2}^{\pi/2} \frac{(1 + e^{x}) x^{2} \cos dx}{(1 + e^{x})}$$

$$2I = \int_{-\pi/2}^{\pi/2} x^2 \cos dx = 2 \int_{0}^{\pi/2} x^2 \cos x \ dx$$

$$I = x^2 \sin x + 2x \cos x - 2 \sin x \Big|_0^{\pi/2}$$

$$I = \frac{\pi^2}{4} - 2 - 0 = \frac{\pi^2}{4} - 2 = \left(\frac{\pi}{\alpha}\right)^2 - \alpha$$

$$\alpha = 2.$$

26. Let A be a 2 \times 2 real matrix and I be the identity matrix of order 2. If the roots of the equation. |A - xI| = 0 be - 1 and 3, then the sum of the diagonal elements of the matrix A^2 is

Ans. 10

 $2x = 6x - x^2$, $x^2 = 4x$, x = 0, 4

Sol.
$$A = \begin{bmatrix} a & b \\ c & d \end{bmatrix} |A - xI| = \begin{vmatrix} a - x & b \\ c & d - x \end{vmatrix}$$

$$|A - xI| = ad - x(a+d) + x^2 - bc$$

$$= x^2 - x(a+d) + ad - bc$$
Given = $(x + 1)(x - 3) = x^2 - 2x - 3$

$$a + d = 2, ad - bc = -3$$

$$A^2 = \begin{bmatrix} a & b \\ c & d \end{bmatrix} \begin{bmatrix} a & b \\ c & d \end{bmatrix} = \begin{bmatrix} a^2 + bc & ab + bd \\ ac + dc & bc + d^2 \end{bmatrix}$$
Sum = $a^2 + bc + bc + d^2 = (a+d)^2 - 2(ad-bc) = 4 + 6 = 10$.

27. If the area of the region $\{(x, y) : 0 \le y \le \min\{2x, 6x - x^2\}\}\$ is A, then 12A is equal to



Sol. $0 \le y \le \min(2x, 6x - x^2)$

Area =
$$\frac{1}{2} \times 4 \times 8 + \int_{4}^{6} 6x - x^{2} dx$$

$$A = 16 + 3x^2 - \frac{x^3}{3} \bigg|_{4}^{6}$$

$$A = 16 + 3(36 - 16) - \frac{(216 - 64)}{3}$$

$$A = 16 + 60 - \frac{152}{3} = 76 - \frac{152}{3} = \frac{228 - 152}{3}$$

$$A = \frac{76}{3}$$

$$12A = 4 \times 76 = 304$$
.

*28. Let the complex numbers α and $\frac{1}{\alpha}$ lie on the circles $|z-z_0|^2=4$ and $|z-z_0|^2=16$ respectively, where $z_0=1+i$. Then, the value of 100 $|\alpha|^2$ is ______

Ans. 20

Sol.
$$|z - z_0|^2 = 4 z_0 = 1 + i$$

$$|z_0| = \sqrt{2}$$

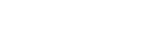
$$(\alpha - 20)(\overline{\alpha} - \overline{z}_0) = 4$$

$$\alpha \overline{\alpha} - \alpha \overline{z}_0 - z_0 \overline{\alpha} + z_0 \overline{z}_0 = 4$$

$$\left|\alpha\right|^2 - \alpha \overline{z}_0 - z_0 \overline{\alpha} + 2 = 4$$

$$\alpha \overline{\mathsf{z}}_0 + \mathsf{z}_0 \overline{\alpha} = \left| \alpha \right|^2 - 2$$

$$\left(\frac{1}{\overline{\alpha}} - z_0\right) \left(\overline{\left(\frac{1}{\overline{\alpha}}\right)} - \overline{z}_0\right) = 16$$



... (i)

$$\begin{split} &\left(\frac{\alpha}{\left|\alpha\right|^{2}}-z_{0}\right)\!\left(\frac{\overline{\alpha}}{\left|\alpha\right|^{2}}-\overline{z}_{0}\right)\!=\!16\\ &\frac{\alpha\overline{\alpha}}{\left|\alpha\right|^{4}}\!-\!\frac{\alpha\overline{z}_{0}}{\left|\alpha\right|^{2}}\!-\!\frac{\overline{\alpha}z_{0}}{\left|\alpha\right|^{2}}\!+z_{0}\overline{z}_{0}=\!16\\ &\frac{1}{\left|\alpha\right|^{2}}\!-\!\frac{\alpha\overline{z}_{0}}{\left|\alpha\right|^{2}}\!-\!\frac{\overline{\alpha}z_{0}}{\left|\alpha\right|^{2}}\!+2=\!16\\ &1\!-\!\alpha\overline{z}_{0}\!-\!\overline{\alpha}\overline{z}_{0}\!+2\left|\alpha\right|^{2}\!=\!6\left|\alpha\right|^{2}\\ &\alpha\overline{z}_{0}\!+\!\overline{\alpha}\overline{z}_{0}=\!1\!-\!14\left|\alpha\right|^{2}\\ &(i)\ \&\ (ii)\\ &|\alpha|^{2}\!-\!2=\!1\!-\!14\left|\alpha\right|^{2}\\ &15\left|\alpha\right|^{2}\!=\!3,\ \left|\alpha\right|\!=\!\frac{1}{5}\ 100|\alpha|^{2}\!=\!20. \end{split}$$

*29. Consider a circle $(x - \alpha)^2 + (y - \beta)^2 = 50$, where α , $\beta > 0$. If the circle touches the line y + x = 0 at the point P, whose distance from the origin is $4\sqrt{2}$, then $(\alpha + \beta)^2$ is equal to _____

Ans. 100
Sol.
$$CP \perp$$
'e to OP

$$\frac{\beta - 4}{\alpha + 4} = 1, \ \beta = \alpha + 8$$

$$CP = 5\sqrt{2}$$

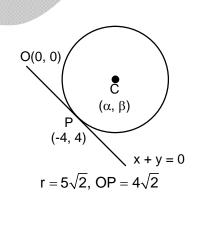
$$\left|\frac{\alpha + \beta}{\sqrt{2}}\right| = 5\sqrt{2}$$

$$\left|2\alpha + 8\right| = 10$$

$$\alpha + 4 \pm 5, \ \alpha = 1, \ \alpha = -9 \text{ (no reallow)}$$

$$\beta = 9$$

$$\left(\alpha + \beta\right)^2 = 100.$$



30. If the solution curve, of the differential equation $\frac{dy}{dx} = \frac{x+y-2}{x-y}$ passing through the point (2, 1) is $\tan^{-1}\left(\frac{y-1}{x-1}\right) - \frac{1}{\beta}\log_e\left(\alpha + \left(\frac{y-1}{x-1}\right)^2\right) = \log_e|x-1|$, then $5\beta + \alpha$ is equal to :

Ans. 11
Sol.
$$\frac{dy}{dx} = \frac{x + y - 2}{x - y}$$

 $x = X + h, y = Y + k$
 $\frac{dy}{dx} = \frac{X + h + Y + k - 2}{X + h - Y - k}$

$$\begin{split} \frac{dy}{dx} &= \frac{X + Y}{X - Y}, \\ h + k - 2 &= 0, \, h - k = 0 \Rightarrow 2h = 2, \, h = 1, \, k = 1 \\ put Y &= vX \\ \frac{dY}{dX} &= v + X \frac{dv}{dX} \\ v + X \frac{dv}{dX} &= \frac{1 + v}{1 - v} \\ X \frac{dv}{dX} &= \frac{1 + v}{1 - v} - v = \frac{1 + v - v(1 - v)}{1 - v} = \frac{1 + v - v + v^2}{1 - v} \\ X \frac{dv}{dX} &= \frac{1 + v^2}{1 - v} \\ \int \frac{1 - v}{1 + v^2} dv &= \int \frac{dX}{X} \\ \int \frac{1}{1 + v^2} dv - \frac{1}{2} \int \frac{2v}{1 + v^2} dv &= \int \frac{dX}{X} \\ \tan^{-1}v - \frac{1}{2} \ln(1 + v^2) &= \ln X + C \\ \tan^{-1}\left(\frac{Y}{X}\right) - \frac{1}{2} \ln\left(1 + \left(\frac{Y}{X}\right)^2\right) &= \ln |x - 1| + C \\ \tan^{-1}\left(\frac{y - 1}{x - 1}\right) - \frac{1}{2} \ln\left(1 + \left(\frac{y - 1}{x - 1}\right)^2\right) &= \ln|x - 1| + C \\ \alpha &= 1, \, \beta = 2, \, 5 \times 2 + 1 = 11. \end{split}$$

PART - B (PHYSICS)

SECTION - A

(One Options Correct Type)

This section contains **20 multiple choice questions**. Each question has **four choices** (1), (2), (3) and (4), out of which **ONLY ONE** option is correct.

*31. A ball suspended by a thread swings in a vertical plane so that its magnitude of acceleration in the extreme position and lowest position are equal. The angle (θ) of thread deflection in the extreme position will be

(1) $2 \tan^{-1} \left(\frac{1}{\sqrt{5}} \right)$

(2) $\tan^{-1}(\sqrt{2})$

(3) 2 $\tan^{-1} \left(\frac{1}{2} \right)$

(4) $\tan^{-1}\left(\frac{1}{2}\right)$

Ans. (3)

Sol. $a_B = g \sin \theta$

. . . (i)

 $a_A = v^2/\ell$

. . . (ii)

. . . (iii)

Applying Work energy theorem

$$\frac{1}{2}mv^2 = mg\ell(1-\cos\theta)$$

$$v^2 = 2q\ell (1 - \cos \theta)$$

Given: $a_A = a_B$

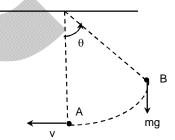
$$\frac{v^2}{\ell} = g \sin \theta$$

 $2(1 - \cos\theta) = \sin\theta$ (using iii)

 $4 \sin^2(\theta/2) = 2 \sin \theta/2 \cos \theta/2$

 $\tan(\theta/2) = \frac{1}{2}$

 $\theta = 2 \tan^{-1} (1/2).$



*32. A bullet is fired into a fixed target looses one third of its velocity after travelling 4 cm. It penetrates further D \times 10⁻³ m before coming to rest. The value of D is:

(1) 3

(2) 2

(3) 4

(4) 5

Ans. (None)

Sol. Velocity becomes 2/3, $v^2 = u^2 + 2as$

 $4v^2/9 = v^2 - 2a \times 4$

 $5v^2/9 = 8a$

 $4v^2/9 = 2aD$

 $D = 3.2 \text{ cm} = 32 \times 10^{-3} \text{ m}$

No options given.

- *33. Given below are two statements: one is labelled as **Assertion (A)** and the other is labelled as **Reason (R)**.
 - **Assertion (A):** The angular speed of the moon in its orbit about the earth is more than angular speed of the earth in its orbit about the sun.
 - **Reason (R):** The moon takes less time to move around the earth than the time taken by the earth to move around the sun.

In the light of the above statements, choose the **most appropriate** answer from the options given below.

Options.

- (1) Both (A) and (R) are correct but (R) is not the correct explanations of (A)
- (2) (A) is not correct but (R) is correct
- (3) Both (A) and (R) are correct and (R) is the correct explanation of (A)
- (4) (A) is correct but (R) is not correct

Ans. (3)

Sol. Time period of earth $T_E = 365$ days

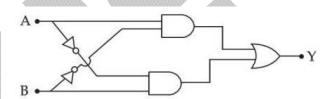
Time period of moon $T_m = 27$ days.

$$T_E > T_m$$

 $\omega_E < \omega_m$

34. The truth table of the given circuit diagram is

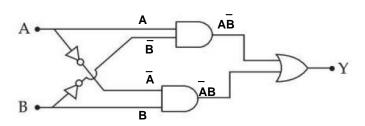
Options



	Α	В	Υ
	A 0 0 1	B 0 1 0	Y 1 1 1 0
(1)	0	1	1
	1	0	1
	1	1	0
	Α	B 0 1 0 1	Υ
	A 0 0 1	0	Y 0 0 0 1
(2)	0	1	0
	1	0	0
	1	1	1
	A 0 0 1 1	B 0 1 0	Y 0 1 1 0
	0	0	0
(3)	0	1	1
	1	0	1
	1	1	0
	Α	В	Υ
	0	0	1
(4)	A 0 0 1	B 0 1 0	Y 1 0 0 1
	1	0	0
	1	1	1

Ans. (3)
Sol.
$$Y = A\overline{B} + \overline{A}B$$

= $A \oplus B$
= XOR gate.



35. The equation of state of a real gas is given by
$$\left(P + \frac{a}{V^2}\right)(V - b) = RT$$
, where P, V and T

are pressure, volume and temperature respectively and R is the universal gas constant. The dimensions of $\frac{a}{b^2}$ is similar to that of:

Ans. (1)

Sol. Dimension of $a = [V^2P]$ Dimension of b = [V]

⇒ Dimension of a/b² has dimension P

*36. A heavy iron bar of weight 12 kg is having its one end on the ground and the other on the shoulder of a man. The rod makes an angle 60° with the horizontal, the weight experienced by the man is:

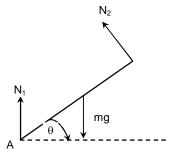
(3)
$$6\sqrt{3}$$
 kg

Ans.

Sol.
$$\tau_A = 0$$

$$N_2 = \frac{mg}{4} = 3g$$

$$N_2 = \frac{mg}{4} = 3g$$



37. Given below are two statements: one is labelled as Assertion (A) and the other is labelled as Reason (R).

Assertion (A): In Vernier calliper if positive zero error exists, then while taking measurements, the reading taken will be more than the actual reading.

Reason (R): The zero error in Vernier Calliper might have happened due to manufacturing defect or due to rough handling.

In the light of the above statements, choose the correct answer from the options given below:

- (1) Both (A) and (R) are correct but (R) is not the correct explanation of (A)
- (2) (A) is false but (R) is true
- (3) (A) is true but (R) is false
- (4) Both (A) and (R) are correct and (R) is the correct explanation of (A)

Ans. (1)

Sol. For positive error measured reading is more than true reading.

38. Wheatstone bridge principle is used to measure the specific resistance (S_1) of given wire, having length (L), radius (r). If X is the resistance of wire, then specific resistance (πr^2)

is;
$$S_1 = X \left(\frac{\pi r^2}{L} \right)$$

If the length of the wire gets doubled then the value of specific resistance will be:

(1)
$$\frac{S_1}{4}$$

(3)
$$\frac{S_1}{2}$$

$$(4) , 2S_1$$

Ans. (2)

Sol. Specific resistance is the property of material.

39. The threshold frequency of a metal with work function 6.63eV is:

(1)
$$16 \times 10^{15}$$
 Hz.

(2)
$$1.6 \times 10^{15}$$
 Hz.

(3)
$$16 \times 10^{12}$$
 Hz.

(4)
$$16 \times 10^{12}$$
 Hz.

Ans. (2)

Sol. $h v_0 = \phi = \text{work function}$

$$v_0 = \frac{6.63 \times 1.6 \times 10^{-19}}{6.63 \times 10^{-34}} Hz$$

$$v_0 = 1.6 \times 10^{15} Hz.$$

40. Primary side of a transformer is connected to 230 V, 50 Hz supply. Turns ratio of primary to secondary winding is 10 : 1. Load resistance connected to secondary side is 46Ω . The power consumed in it is:

Ans. (2)

Sol.
$$\frac{V_1}{V_2} = \frac{n_1}{n_2} = 10$$

$$V_2 = \frac{V_1}{10} = 23V$$

$$P = \frac{V_2^2}{R} = \frac{23 \times 23}{46} = 11.5W$$

*41. Given below are two statements:

Statement (I): The limiting force of static friction depends on the area of contact and independent of materials.

Statement (II): The limiting force of kinetic friction is independent of the area of contact and depends on materials.

In the light of the above statements, choose the most appropriate answer from the options given below:

Options

- (1) Both Statement I and Statement II are incorrect
- (2) Both Statement I and Statement II are correct
- (3) Statement I is correct but Statement II is incorrect
- (4) Statement I is incorrect but Statement II is correct.

Ans. (4)

Sol. Both static and kinetic frictions are independent of area of contact.

- 42. A current of 200 μ A deflects the coil of a moving coil galvanometer through 60°. The current to cause deflection through $\frac{\pi}{10}$ radian is :
 - (1) 120 μA

(2) 180 μA

(3) $30 \mu A$

(4) 60 μA

Ans. (4)

Sol. $\theta = \left(\frac{\mathsf{nBA}}{\mathsf{k}}\right)\mathsf{I}$

For I = 200 μ A, $\theta = \pi/3$ $\Rightarrow \pi/3 = \left(\frac{\text{nBA}}{200 \mu\text{A}}\right) 200 \mu$ A

. . . (i)

For $\theta = \pi/10$

$$I = \frac{\theta}{(\mathsf{nBA/k})} = \frac{\pi/10}{\pi/600} \,\mu\mathsf{A}$$

 $I = 60 \mu A$

- *43. The total kinetic energy of 1 mole of oxygen at 27° C is : [Use universal gas constant (R) = 8.31J/ mole K]
 - (1) 6232.5 J

(2) 6845.5J

(3) 5670.5 J

(4) 5942.0 J

Ans. (1)

Sol. Total Kinetic energy = $\frac{f}{2}$ nRT (f = 5, T = 300 K)

TE = 6232.5 J

- *44. During an adiabatic process, the pressure of a gas is found to be proportional to the cube of its absolute temperature. The ratio of $\frac{C_p}{C_V}$ for the gas is:
 - (1) $\frac{7}{5}$

(2) $\frac{9}{7}$

(3) $\frac{5}{3}$

(4) $\frac{3}{2}$

Ans. (4)

Sol. $P \propto T^3$

 \Rightarrow P = kT³ (k is constant)

 \Rightarrow PV^{3/2} = const.

 \Rightarrow $C_p/C_v = 3/2$

45. The atomic mass of $_6C^{12}$ is 12.000000u and that of $_6C^{13}$ is 13.003354u . The required energy to remove a neutron from $_6C^{13}$, if mass of neutron is 1.008665u , will be :

(1) 6.25 MeV

(2) 49.5 MeV

(3) 4.95 MeV

(4) 62.5 MeV

Ans. (3)

Sol. Mass defect = |13.003354 - (12 + 1.008665)| u

 $\Delta m = 0.005311 \text{ u}$

 $E = \Delta mc^2 = 0.00511 \times 931.5 \text{ MeV}$

E = 4.95 MeV

*46. Given below are two statements : one is labelled as **Assertion (A)** and the other is labelled as **Reason (R)**.

Assertion (A): The property of body, by virtue of which it tends to regain its original shape when the external force is removed, is Elasticity.

Reason (R): The restoring force depends upon the bonded inter atomic and inter molecular force of solid.

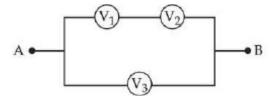
In the light of the above statements, choose the **correct** answer from the options given below :

Options

- (1) Both (A) and (R) are true and (R) is the correct explanation of (A)
- (2) (A) is true but (R) is false
- (3) (A) is false but (R) is true
- (4) Both (A) and (R) are true but (R) is not the correct explanation of (A)

Ans. (1)

- **Sol.** The restoring force is dependent on the bonded interatomic and intermolecular force of solid.
- 47. Three voltmeters, all having different internal resistances are joined as shown in figure. When some potential difference is applied across A and B, their readings are V_1 , V_2 and V_3 . Choose the correct option.



- (1) $V_1 \neq V_3 V_2$
- (3) $V_1 + V_2 = V_3$

(2) $V_1 + V_2 > V_3$ (4) $V_1 = V_2$

Ans. (3)

Sol. The parallel branches have same potential difference $V_1 + V_2 = V_3$ (also, using KVL)

48. Given below are two statements : one is labelled as **Assertion (A)** and the other is labelled as **Reason (R)**.

Assertion (A): Work done by electric field on moving a positive charge on an equipotential surface is always zero.

Reason (R): Electric lines of forces are always perpendicular to equipotential surfaces. In the light of the above statements, choose the most appropriate answer from the options given below:

Options:

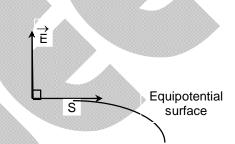
- (1) (A) is not correct but (R) is correct
- (2) (A) is correct but (R) is not correct
- (3) Both (A) and (R) are correct and (R) is the correct explanation of (A)
- (4) Both (A) and (R) are correct but (R) is not the correct explanation of (A)

Ans. (3)

Sol. $W = Q\Delta V$

For equipotential surface $\Delta V = 0$ $\Rightarrow W = 0$

The electric field lines are perpendicular to equipotential surfaces.



- 49. An object is placed in a medium of refractive index 3. An electromagnetic wave of intensity $6 \times 10^8 \text{ W/m}^2$ falls normally on the object and it is absorbed completely. The radiation pressure on the object would be (speed of light in free space = $3 \times 10^8 \text{m/s}$):
 - (1) 2 Nm⁻²

(2) 6 Nm⁻²

(3) 36 Nm⁻²

(4) 18 Nm⁻²

Ans. (2)

- **Sol.** Radiation press P = $\frac{1}{(c / \mu)} = 6 \text{Nm}^{-2}$
- 50. When a polaroid sheet is rotated between two crossed polaroids then the transmitted light intensity will be maximum for a rotation of :
 - $(1) 90^{\circ}$

(2) 45^{0}

(3) 30°

 $(4) 60^{\circ}$

Ans. (2)

Sol. $I = I_0 \cos^2 \phi \sin^2 \phi = \frac{I_0}{4} \sin^2 \{2\phi\}$

For maximum I, $2\phi = \pi/2$

 $\varphi=\pi/4$

SECTION - B

(Numerical Answer Type)

This section contains 10 Numerical based questions. The answer to each question is rounded off to the nearest integer value.

*51. A closed organ pipe 150 cm long gives 7 beats per second with an open organ pipe of length 350 cm, both vibrating in fundamental mode. The velocity of sound ism/s

Ans. 294

Sol.
$$v_1 = \frac{v}{4\ell_1}$$

$$v_2 = \frac{v}{2\ell_2}$$

$$v_1 - v_2 = 7$$

$$\Rightarrow \frac{v}{2} \left[\frac{1}{2\ell_1} - \frac{1}{\ell_2} \right] = 7$$

$$v = 294 \text{ m/s}.$$

Ans. 8

Sol.
$$Q = 50 \times 1.6 \times 10^{-19} \text{ C}$$

 $\Rightarrow Q = 8 \times 10^{-18} \text{ C}$
 $V = \frac{kQ}{R} = \frac{9 \times 10^9 \times 8 \times 10^{-18}}{9 \times 10^{-15}} = 8 \times 10^6 \text{ V}$

Ans. 45

Sol.
$$S = ut + \frac{1}{2}at^2$$
 u_0 $S_{AB} = 80 = u_A \times 2 + 5 \times 2^2$ $\Rightarrow u_A = 30 \text{ m/s}$ $\Rightarrow u_A^2 = u_0^2 + 2 \times 10 \times S_{OA} \quad (u_0 = 0)$ $\Rightarrow S_{OA} = 45 \text{ m}$

*54. A ring and a solid sphere roll down the same inclined plane without slipping. They start from rest. The radii of both bodies are identical and the ratio of their kinetic energies is $\frac{7}{x}$, where x is

Ans. Data incomplete

Sol. Masses of ring and sphere were not given.

55. A series LCR circuit with L = $\frac{100}{\pi}mH$, $C = \frac{10^{-3}}{\pi}F$ and R = 10Ω , is connected across an ac source of 220V, 50Hz supply. The power factor of the circuit would be

Sol.
$$z = \sqrt{R^2 + \left(\omega L - \frac{1}{\omega C}\right)^2}$$

$$\omega L = 2\pi \times \frac{100}{\pi} \times 10^{-3} \times 50 = 10, R = 10$$

$$\frac{1}{\omega C} = \frac{1}{2\pi \times 50 \times 10^{-3}} \Rightarrow 10$$

$$Z = R$$

$$\cos \phi = 1, (p. f. = 1)$$

56. A parallel beam of monochromatic light of wavelength 5000Å is incident normally on a single narrow slit of width 0.001mm. The light is focused by convex lens on screen, placed on its focal plane. The first minima will be formed for the angle of diffraction of (degree).

Ans. 30

Sol.
$$d \sin \theta = \lambda$$
 for first minima $1 \times 10^{-6} \sin \theta = 5 \times 10^{-7}$ $\sin \theta = \frac{1}{2}$ $\theta = 30^{0}$

57. Two charges of -4μ C and $+4\mu$ C are placed at the points A(1, 0, 4) m and B(2, -1, 5) m located in an electric field $\vec{E} = 0.20\hat{i}$ V / cm. The magnitude of the torque acting on the dipole is $8\sqrt{\alpha} \times 10^{-5}$ Nm, where $\alpha =$

Sol.
$$\vec{r}_A = \hat{i} + 4\hat{k}$$

 $\vec{r}_B = 2\hat{i} - \hat{j} + 5\hat{k}$
 $\vec{P} = q(\vec{r}_B - \vec{r}_A)$
 $\vec{P} = 4 \times 10^{-6} (\hat{i} - \hat{j} + \hat{k})$
 $\vec{E} = 20 \hat{i} \text{ V/m}$
 $\vec{\tau} = \vec{P} \times \vec{E} = 8 \times 10^{-5} (\hat{k} + \hat{i}) = 8\sqrt{2} \times 10^{-5} \text{ Nm.}$
 $\alpha = 2$

58. If Rydberg's constant is R, the longest wavelength of radiation in Paschen series will be $\frac{\alpha}{7R}$ where α =

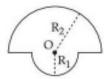
Ans. 144

Sol.
$$\frac{1}{\lambda} = R \left[\frac{1}{n_1^2} - \frac{1}{n_2^2} \right],$$

$$n_1 = 3, n_2 = 4$$

$$\frac{1}{\lambda} = R \left[\frac{1}{9} - \frac{1}{16} \right] \implies \lambda = \frac{144}{7R}, \alpha = 144$$

59. The magnetic field at the centre of a wire loop formed by two semi-circular wires of radii $R_1=2\pi$ m and $R_2=4\pi$ m, carrying current I=4A as per figure given below is $\alpha \times 10^{-7}T$. The value of α is (Centre O is common for all segments)



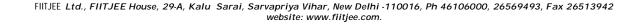
Ans. 3

Sol. B = B₁ + B₂ =
$$\frac{\mu_0 \text{NI}}{2} \left(\frac{1}{r_1} + \frac{1}{r_2} \right) = \frac{4\pi \times 10^{-7} \times 4}{2} \left[\frac{1}{2\pi} + \frac{1}{4\pi} \right] = 3 \times 10^{-7} \text{T}$$

*60. The reading of pressure metre attached with a closed pipe is $4.5 \times 10^4 \,\text{N/m}^2$. On opening the valve, water starts flowing and the reading of pressure metre falls to $2.0 \times 10^4 \,\text{N/m}^2$. The velocity of water is found to be \sqrt{V} m/s. The value of V s

Sol.
$$\frac{1}{2}\rho v^2 + P = P_0$$

$$\frac{1}{2} \times 10^3 (v^2) = P_0 - P = 2.5 \times 10^4 \Rightarrow v = \sqrt{50} \text{ , so, } V = 50$$



PART - C (CHEMISTRY)

SECTION - A

(One Options Correct Type)

This section contains **20 multiple choice questions**. Each question has **four choices** (1), (2), (3) and (4), out of which **ONLY ONE** option is correct.

61. Given below are two statements:

Statement (I): Oxygen being the first member of group 16 exhibits only-2 oxidation state. Statement (II): Down the group 16 stability of +4 oxidation state decreases and +6 oxidation state increases.

In the light of the above statements, choose the most appropriate answer from the options given below:

- (1) Both Statement I and Statement II are incorrect
- (2) Statement I is correct but Statement II is incorrect
- (3) Statement I is incorrect but Statement II is correct
- (4) Both Statement I and Statement II are correct

Ans. (1)

Sol. Both the statements are wrong.

62. Phenolic group can be identified by a positive :

(1) Phthalein dye test

(2) Carbylammine test

(3) Tollen's test

(4) Lucas test

Ans. (1)

Sol. In pthalein dye test, phenol gives pink colour due to formation of phenolphthalein in basic medium.

63. Major product formed in the following reaction is a mixture of :

Ans. (2)

$$\begin{array}{c|c} CH_3 & H & CH_3 \\ \hline O - C - CH_3 & O - C - CH_3 \\ \hline CH_3 & & & \\ \hline \\ I - C(CH_3)_3 & & & \\ \hline \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & &$$

Hence, major product is given in option (2).

- 64. Which structure of protein remains intact after coagulation of egg white on boiling?
 - (1) Tertiary

(2) Secondary

(3) Quaternary

(4) Primary

Ans. (4)

Sol. Primary structure of protein remains intact after coagulation of egg.

- *65. Which of the following cannot function as an oxidizing agent?
 - (1) MnO₄

(2) SO_4^2

(3) N^{3-}

(4) BrO₂

Ans. (3)

- **Sol.** N³- is in its lowest oxidation state. Hence, it can not undergo reduction. So can not act as an oxidisiing agent.
- *66. The incorrect statement regarding conformations of ethane is:
 - (1) Eclipsed conformation is the most stable conformation
 - (2) Ethane has infinite number of conformations
 - (3) The conformations of ethane are inter-convertible to one-another
 - (4) The dihedral angle in staggered conformation is 60°

Ans. (1)

Sol. Eclipsed conformation is the least stable conformation.

67. Choose the correct option having all the elements with d¹⁰ electronic configuration from the following

(1) ²⁷Co, ²⁸Ni, ²⁶Fe, ²⁴Cr

(2) 46 Pd, 28 Ni, 26 Fe, 24 Cr

(3) ²⁹Cu, ³⁰Zn, ⁴⁸Cd, ²⁷Ag

(4) ²⁸Ni, ²⁴Cr, ²⁶Fe, ²⁹Cu

Ans. (3)

Sol. Only option (3) is having all the elements in d¹⁰ electronic configuration.

68. Given below are two statements:

Statement (I): In the Lanthanoids the formation Ce⁺⁴ is favoured by its noble gas configuration

Statement (II): Ce⁺⁴ is a strong oxidant reverting to the common +3 state

In the light of the above statements, choose the most appropriate from the options given below:

- (1) Both Statement I and Statement II are true
- (2) Both Statement I and Statement II are false
- (3) Statement I is false but Statement II is true
- (4) Statement I is true but Statement II is false

Ans. (1)

Sol. Both the statements are correct.

- *69. The technique used for purification of steam volatile water immiscible substance is :
 - (1) steam distillation

- (2) distillation
- (3) fraction distillation under reduced pressure (4) fractional distillation

Ans. (1)

Sol. Steam distillation is used for purification of steam volatile water immiscible substances.

- 70. The molecular formula of second homologue in the homologous series of mono carboxylic acid is
 - (1) $C_2H_4O_2$

(2) C₃H₆O₂

(3) CH₂O

(4) C₂H₂O₂

Ans. (1)

Sol. Acetic acid will be second homologue in the homologous series of mono carboxylic acids.

- 71. Which of the following statements is not correct about rusting of iron?
 - (1) Coating of iron surface by tin prevents rusting, even if the tin coating is peeling off.
 - (2) Dissolved acidic oxides SO₂, NO₂ in water act as catalyst in the process of rusting.
 - (3) When pH lies above 9 or 10, rusting of iron does not take place
 - (4) Rusting of iron is envisaged as setting up of electrochemical cell on the surface of iron object.

Ans. (1)

Sol. Tin is having lower standard oxidation potential than Fe. Hence, Sn can not prevent rusting of iron, if its coating is peeled off.

72. Match List I with List II

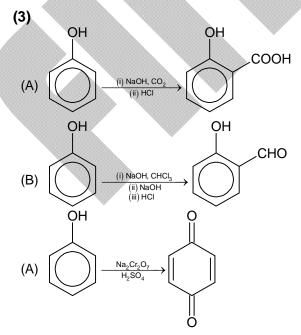
List –I (Reaction)		List-II (Reagent(s)		
(A)	OH _	СООН	(1)	Na ₂ Cr ₂ O ₇ ,H ₂ SO ₄
	ŌН	ОН	(II)	(i)NaOH (ii) CH ₃ Cl
(B)		СНО		
(C)	OH		(III)	(i)NaOH,CHCl ₃ (ii) NaOH (iii) HCl
(D)	OH	OCH ₃	(IV)	(i)NaOH (ii) CO ₂ (iii)HCl

Choose the correct answer from the options given below:

$$\begin{array}{lll} \text{(1) } (A) - (II), \ (B) - (I), \ (C) - (III), \ (D) - (IV) & \text{(2) } (A) - (IV), \ (B) - (I), \ (C) - (III), \ (D) - (II) \\ \text{(3) } (A) - (IV), \ (B) - (III), \ (C) - (I), \ (D) - (II) & \text{(4) } (A) - (II), \ (B) - (III), \ (C) - (I), \ (D) - (IV) \end{array}$$

(3)
$$(A) - (IV)$$
, $(B) - (III)$, $(C) - (I)$, $(D) - (II)$ $(A) - (II)$, $(B) - (III)$, $(C) - (I)$, $(D) - (IV)$

Ans. Sol.



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(A)
$$(i) \xrightarrow{\text{NaOH}} (i) \xrightarrow{\text{OCH}_3}$$

- 73. Identify from the following species in which d²sp³ hybridization is shown by central atom:
 - (1) BrF₅

(2) $\left[\text{Co}(\text{NH}_3)_6 \right]^{3+}$

(3) $\left[Pt(Cl_4) \right]^{2-}$

(4) SF₆

Ans. (2)

Sol. $\left[\text{Co(NH}_3)_6 \right]^{3+}$ will form inner orbital complex. Hence its hybridization will be d^2sp^3 .

74. Identify B formed in the reaction

$$CI - (CH_2)_4 - CI \xrightarrow{excess NH_3} A \xrightarrow{NaOH} B + H_2O + NaCI$$

(1) $CINH_3 - (CH_2)_4 - NH_3CI^-$

(2)

(3) $H_2N - (CH_2)_4 - NH_2$

(4)

Ans. (3) Sol.

$$CI - (CH_2)_4 - CI \xrightarrow{\text{Excess}} CIH_3N - (CH_2)_4 - NH_3CI$$

$$\downarrow NAOH$$

$$\downarrow NAOH$$

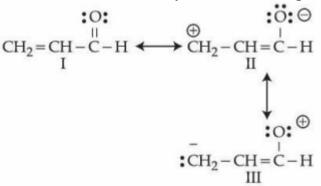
75. Bond line formula of HOCH(CN)₂ is

(4)
$$HO-CH$$
 $C \equiv N$
 $C \equiv N$

Ans. (3)

Correct representation of bond line formula for given compound is Sol.

*76. The order of relative stability of the contributing structure is:



Choose the correct answer from the option given below:

(1) | > | > | |

(2) I = II = III

(3) | | | > | > |

(4) || > | > ||

Ans. (1)

- Sol. (i) Neutral > charged
 - (ii) Positive charge on electropositive and negative on electronegative atom is more stable.

| > | > | |

- The quantity which changes with temperature is : *77.
 - (1) Mole fraction

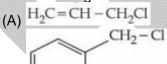
(2) Molarity

(3) Mass percentage

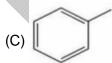
(4) Molality

Ans. (2)

- Sol. Molarity depends upon volume of solution, which changes with temperature.
- 78. Which among the following halide/s will not show S_N1 reaction:



(B)
$$CH_3 - CH = CH - CI$$



(D)
$$H_3C$$
 CH – CI

Choose the most appropriate answer from the options given below:

(1) (A), (B) and (D) only

(2) (B) and (C) only

(3) (B) only

(4) (A) and (B) only

Ans. (3)

Vinylic carbocation is highly unstable. So, it does not show S_N1 reaction. Sol.

- 79. Identify the incorrect pair from the following
 - (1) Polythene preparation -TiCl₄, Al(CH₃)₃
 - (2) Photography AgBr
 - (3) Haber process -Iron
 - (4) Wacker process -Pt Cl₂
- Ans. (4)
- **Sol.** In the wacker process, PdCl₂ is used as catalyst.
- *80. The final product A, formed in the following reaction sequence is:

Ans. (4) Sol.

$$\begin{array}{c} \text{Ph--CH=-CH}_2 \xrightarrow{\text{(i) BH}_3} \text{Ph---CH}_2 \xrightarrow{\text{CH}_2} \text{Ph---CH}_2 \xrightarrow{\text{HBr}} \text{Ph---CH}_2 \xrightarrow{\text{CH}_2} \\ \text{Mg} & \text{Ether} \end{array}$$

SECTION - B

(Numerical Answer Type)

This section contains 10 Numerical based questions. The answer to each question is rounded off to the nearest integer value.

81. The hydrogen electrode is dipped in a solution of pH = 3 at 25° C. The potential of the electrode will be $\times 10^{-2}$.

$$\left(\frac{2.303RT}{F} = 0.059 \text{ V}\right)$$

Sol.
$$2H^+ + 2e^- \longrightarrow H_2(g)$$

 $E_{H^+/H_2} = 0$
Given pH = 3
 $\therefore [H^+] = 10^{-3}$

$$E_{H^{+}/H_{2}}^{0} = 0 - \frac{0.0591}{2} log \frac{pH_{2}}{[H^{+}]^{2}}$$

$$= -\frac{0.0591}{2} log \frac{1}{10^{-6}}$$

$$= -\frac{0.0591}{2} \times 6$$

$$= -0.0591 \times 3 V$$

$$= -0.1773 V$$

$$= 17.7 \times 10^{-2} V$$

Nearest integer is 18.

- *82. Volume of 3 M NaOH (formula weight 40 g mol⁻¹) which can be prepared from 84 g of NaOH is $____ \times 10^{-1}$ dm³.
- Ans. 7
- **Sol.** Number of moles of NaOH = $\frac{84 \text{ g}}{40 \text{ g/mol}}$

= 2.1 moles

Let the volume be x dm³

 M_1V_1 = number of moles = 2.1

$$\Rightarrow$$
 3 × x = 2.1

$$x = 0.7 \text{ dm}^3 = 7 \times 10^{-1} \text{ dm}^3$$

- 83. Total number of ions from the following with noble gas configuration is _____ . $Sr^{2+}(z=38)$, $Cs^{+}(z=55)$, $La^{2+}(z=57)$, $Pb^{2+}(z=82)$, $Yb^{2+}(z=70)$ and $Fe^{2+}(z=26)$
- Ans. 2

Sol. Sr²⁺ and Cs⁺ are having noble gas configuration.

- 84. The spin only magnetic moment value of square planar complex $\left[Pt(NH_3)_2 Cl(NH_2CH_3) \right] Cl$ is B.M. (Nearest integer) (Given atomic number for Pt = 78)
- Ans. 0

- *85. 9.3 g of aniline is subjected to reaction with excess of acetic anhydride to prepare acetanilide. The mass of acetanilide produced if the reaction is 100% completed is $____ \times 10^{-1}$ g. (Given molar mass in g mol⁻¹ N : 14, O : 16, C : 12, H = 1)
- Ans. 135

Sol.

Mass 9.3 g

moles
$$\frac{9.3}{93} = 0.1$$

Mass of product formed will be $0.1 \times \text{molar mass of acetanilide} = 0.1 \times 135 \text{ g}$ $= 13.5 g = 135 \times 10^{-1} g$

*86. For a certain thermochemical reaction $M \to N \text{ at } T = 400 \text{ K}, \Delta H^{\odot} = 77.2 \text{ kJ mol}^{-1}, \Delta S = 122 \text{ JK}^{-1}$ log equilibrium constant (log K) is ____

Ans. 37

Ans. 37
Sol.
$$\Delta G^0 = \Delta H^0 - T\Delta S^0$$
 $\Delta G = \Delta G^0 + RT \ln K_{eq}$
 $\Delta G^0 = -RT \ln K_{eq}$
 $\Delta G^0 = 77.2 \text{ kJ/mol} - 400 \times 0.122 \text{ kJ/mol}$
 $= 77.2 \text{ kJ/mol} - 48.8 \text{ kJ/mol} = 28.4 \text{ kJ/mol}$
 $28.4 \text{ kJ/mol} = -8.314 \times 400 \text{ ln K}$

$$\Rightarrow \ln K = -\frac{28400}{8.314 \times 400}$$

$$\Rightarrow 2.303 \log K = -\frac{284}{8.314 \times 400}$$

$$\Rightarrow \ln K = -\frac{284}{8.314 \times 400}$$

$$\Rightarrow 2.303 \log K = -\frac{284}{8.314 \times 400}$$

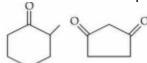
$$\Rightarrow -37.08 \times 10^{-1}$$

*87. 1 mole of PbS is oxidized by 'X' moles of O_3 to get 'Y' moles of O_2 , X + Y = _____

Ans.

Sol. The balanced chemical eqaution is $PbS + 2O_3 \longrightarrow PbSO_4 + O_2$ X is 2 and Y is 1. So, X + Y = 2 + 1 = 3

*88. Total number of compounds with Chiral carbon atoms from following is ...

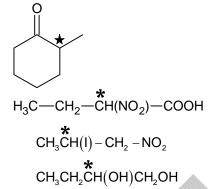


$$CH_3 - CH_2 - CH(NO_2) - COOH$$

 $CH_3 - CH_2 - CHBr - CH_2 - CH_3$
 $CH_3 - CH(I) - CH_2 - NO_2$
 $CH_3 - CH_2 - CH(OH) - CH_2OH$
 $CH_3 - CH - CH(I) - C_2H_5$

Ans. 5

Sol. The compounds with chiral atoms are:



 $\begin{array}{c} \mathsf{H_3C-}\overset{\color{red}\star}{\mathsf{CH}}-\overset{\color{red}\star}{\mathsf{CH}}(\mathsf{I})-\mathsf{C}_2\mathsf{H}_5\\ |\\|\\|\end{array}$

89. Time required for completion of 99.9 % of a first order reaction is _____ times of half life.

 $(t_{1/2})$ of the reaction

Ans. 10

Sol. $kt = 2.303 \log \frac{a_o}{a_t}$

$$t = \frac{2.303}{\frac{\ln 2}{t_{1/2}}} \log \frac{a_o}{a_t}$$

$$\Rightarrow t_{99.9\%} = \frac{2.303}{0.693} t_{1/2} \log \frac{100}{0.1}$$

$$=\frac{2.303}{0.693}.3.t_{1/2}\simeq10$$

*90. The number of non-polar molecules from the following is ______.

$$\mathsf{HF}, \mathsf{H}_2\mathsf{O}, \mathsf{SO}_2, \mathsf{H}_2, \mathsf{CO}_2, \mathsf{CH}_4, \mathsf{NH}_3, \mathsf{HCl}, \mathsf{CHCl}_3, \mathsf{BF}_3$$

Ans. 4

Sol. The non polar molecules are H_2 , CO_2 , CH_4 and BF_3 .